

# Information Interaction Profile of Choice Adoption

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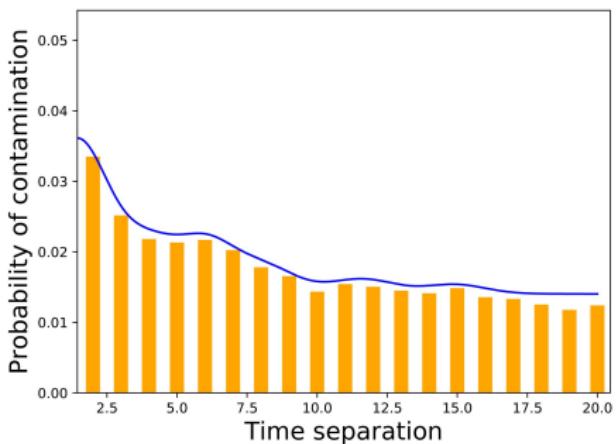
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# Problem and definitions

- “Information Interaction Profile of Choice Adoption”
  - ◊ Information : a tweet, a situation, an ad, etc.
  - ◊ Choice adoption : a retweet, a reaction, a click, etc.
  - ◊ Interaction profile : how the exposure to a first piece of information affect a user's choice on a later one according to time.

# Problematic

- We are looking for trends in information interaction : how does it evolve with time, and does it take place between every piece of information ?



**Figure 1 – Interaction profile – Probability of clicking a Twitter URL after seeing a Migré URL**

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## Previous works

- Info-info interaction :
  - ◊ Clash of the Contagions [1] – Models interactions as modulations over a pre-computed virality ; considers each time interval separately ; SGD
  - ◊ IMMSBM [2] – Models symmetric interaction with no assumption on virality ; does not consider time ; EM
- Other types of interaction :
  - ◊ Information overload [3]
  - ◊ Users' attention [4]
  - ◊ Topic-dependent networks [5]

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# The data

- Users are exposed to pieces of information (light squares).
- Sometimes, they will act on one of them after being exposed (orange squares).
- The action takes place a time  $t_s$  after the exposure.
- The time separating exposures can be constant (order of exposition) or vary (absolute exposure times).

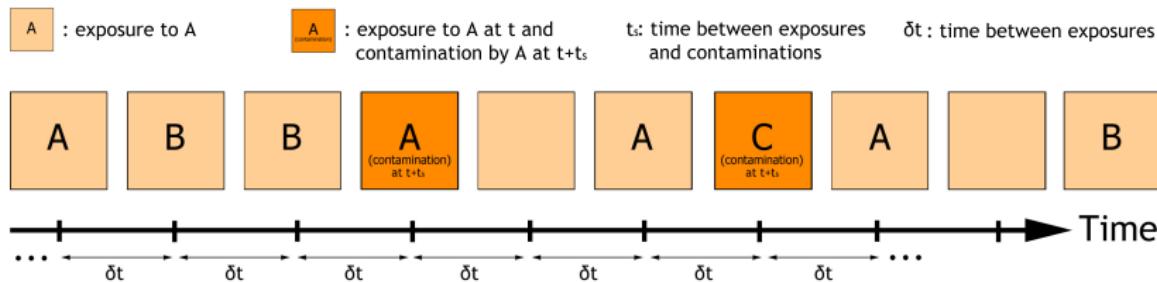


Figure 2 – Illustration of the interacting process

# Assumptions

- This modeling comes with several assumptions :
  - ◊ Pieces of information appear independently from each other (unfit for survival or Hawkes modeling, in particular the system is not self-exciting)
  - ◊ A user's action is conditioned by previous exposures only (as in [1, 6]).
  - ◊  $t_s$  is constant (i.e. the time between a read and a retweet in the case of Twitter). This hypothesis is a simplification for clarity of presentation and can be easily alleviated.

# The model

- Data  $\mathcal{D} \equiv \{(t_i^{(x)}, c_{t_i}^{(x)}, \mathcal{H}_i^{(x)})\}_{i,x}$  with :
  - ◊  $t_i^{(x)}$  :  $i^{th}$  exposure to  $x$  at time  $t_i + t_s$
  - ◊  $c_{t_i}^{(x)}$  : whether the user act on the exposure
  - ◊  $\mathcal{H}_i^{(x)}$  : history of exposures prior to  $t_i^{(x)}$
- Log-likelihood :

$$\ell(\beta | \mathcal{D}, t_s) = \sum_{\mathcal{D}} \sum_{t_j^{(y)} \in \mathcal{H}_i^{(x)}} c_{t_i}^{(x)} \log \left( H(t_i^{(x)} + t_s | t_j^{(y)}, \beta_{xy}) \right) \\ + (1 - c_{t_j}^{(y)}) \log \left( 1 - H(t_i^{(x)} + t_s | t_j^{(y)}, \beta_{xy}) \right) \quad (1)$$

- $H(t_i^{(x)} + t_s | t_j^{(y)}, \beta_{xy})$  is the instantaneous probability of action on  $x$  at time  $t_i^{(x)} + t_s$  given an exposure to  $y$  at  $t_j^{(y)}$ .
- $H$  is a time varying kernel function parametrized by the information interaction matrix  $\beta$ .

# Optimization

- $\ell(\beta|\mathcal{D}, t_s)$  can be split in as many subproblems as there are pieces of information. Input data for each of them :  
$$\mathcal{D}^{(x)} \equiv \{(\mathcal{H}_i^{(x)}, t_i^{(x)}, c_{t_i}^{(x)})\}_i$$
- $\ell(\beta|\mathcal{D}, t_s)$  is convex if

$$\left\{ \begin{array}{l} H'^2 \geq H''H \\ H'^2 \geq -H''(1-H) \\ H \in ]0; 1[ \end{array} \right. \quad (2)$$

- A number of kernel functions satisfy convexity : exponential, Rayleigh, power-law, gaussian, linear combination of those.
- Final problem :  $\min_{\beta \geq 0} -\ell(\beta|\mathcal{D}, t_s)$

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# Datasets

- Synthetic (20.000 sequences of length 50 steps)
- Twitter dataset (104,349 sequences of average length 53.5 steps, exposure are tweets and contagions are retweets) [7]
- Iterated Prisoner's dilemma dataset (2,337 sequences of average length 9.0 steps, exposures are situations, contagions are players choices) [8, 9]
- Ads dataset (87,500 sequences of average length 23.9 steps, exposures are ads, contagions are clicks on ads) [10].

## Background noise

- A background noise is induced due to the data gathering process : random correlations.

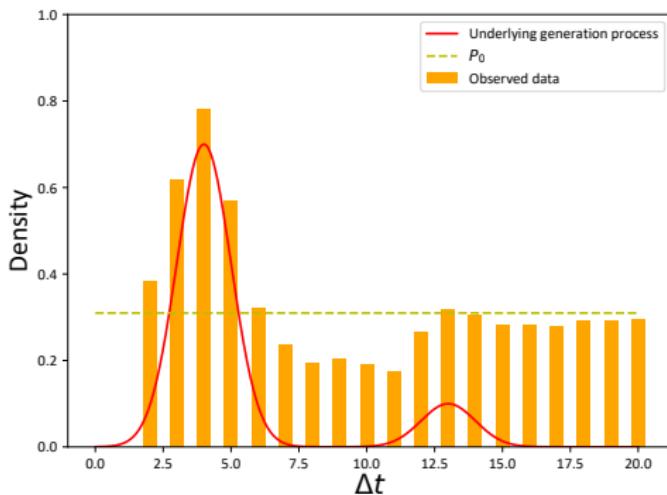


Figure 3 – Illustration of the background noise on synthetic data

# Kernel choice

- We choose 2 different kernels :
  - ◊ InterRate-EXP (exponential kernel) :
$$\log H(t_i^{(x)} + t_s | t_j^{(y)}, \beta_{xy}) = -\beta_{ij}^{(bg)} - \beta_{ij}(t_i + t_s - t_j)$$
  - ◊ InterRate-RBF (Gaussian kernel) :
$$\log H(t_i^{(x)} + t_s | t_j^{(y)}, \beta_{ij}) = -\beta_{ij}^{(bg)} - \sum_{s=0}^S \frac{\beta_{ij}^{(s)}}{2} (t_i + t_s - t_j - s)^2$$
- The time-independent component of both kernels  $\beta_{ij}^{(bg)}$  fits the background noise, while other parameters fit temporal dynamics.

## Baselines

- ICIR – Version of InterRate without interactions : off-diagonal entries of  $\beta$  are null. We use a RBF kernel.
- Clash of the contagions (CoC) [1] – considers each time-bin separately
- IMMSBM [2] – does not consider temporal aspect ; enforces symmetry  $\beta_{ab} = \beta_{ba}$
- Naive – Time-independent frequency of action for each pair of pieces of information.
- We split data into training and test sets (80%-20%) and perform a 5-fold cross validation. We compare the inferred and true interaction profiles using the residual sum of squares (RSS), Jensen-Shanon (JS) divergence and the best-case F1-score (BCF1).

## Comparison on synthetic data

- Note that InterRate as such aims to describe the process, not to make predictions (background noise included in evaluation)

		RSS	JS div.	BCF1	MSE $\beta$
Synth-20	IR-RBF	18.4151	0.002 28	0.919	0.001
	ICIR	139.5926	0.009 98	0.827	0.016
	Naïve	145.5132	0.010 38	0.822	
	CoC	123.0583	0.009 38	0.822	
	IMMSBM	222.0555	0.017 29	0.727	
Synth-5	IR-RBF	0.1169	0.000 22	0.974	0.005
	ICIR	8.2661	0.008 12	0.850	0.019
	Naïve	10.0264	0.009 96	0.821	
	CoC	0.1154	0.000 20	0.976	
	IMMSBM	11.6936	0.013 62	0.769	

Figure 4 – Numerical results for synthetic data

# Comparison on real-world data

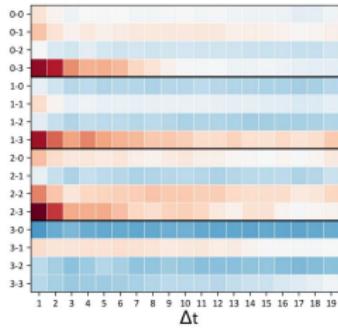
		RSS	JS div.	BCF1
Twitter	IR-RBF	0.0015	0.000 06	0.983
	IR-EXP	0.0011	0.000 05	0.986
	ICIR	0.0137	0.000 63	0.961
	Naïve	0.0161	0.000 73	0.938
	CoC	0.0017	0.000 07	0.957
	IMMSBM	0.0147	0.000 68	0.954
PD	IR-RBF	1.1268	0.007 58	0.979
	IR-EXP	1.5526	0.008 67	0.966
	ICIR	3.5359	0.018 23	0.938
	Naïve	3.6527	0.019 15	0.945
	CoC	1.2409	0.008 09	0.974
	IMMSBM	20.3773	0.087 01	0.767
Ads	IR-RBF	0.0043	0.000 04	0.981
	IR-EXP	0.0030	0.000 03	0.985
	ICIR	0.0983	0.000 85	0.966
	Naïve	0.1453	0.001 26	0.913
	CoC	0.0045	0.000 05	0.974
	IMMSBM	0.0155	0.000 15	0.954

Figure 5 – Numerical results on real-world data

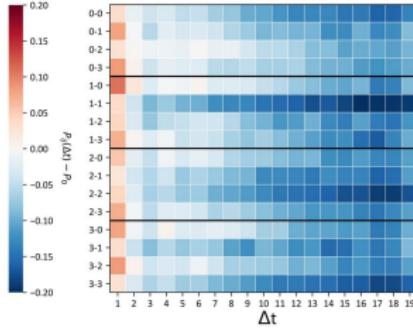
# Visualization

- We plot the intensity of interactions in time (probability of action minus inferred background noise) for every dataset.
- We recover SotA conclusions :
  - ◊ Twitter : most informative URL interactions occur within the 3 time steps [1], and interactions are weak [1, 2]. Interactions are sparse [2].
  - ◊ Ads : globally decreasing probability of click when two exposures are distant in time [10].

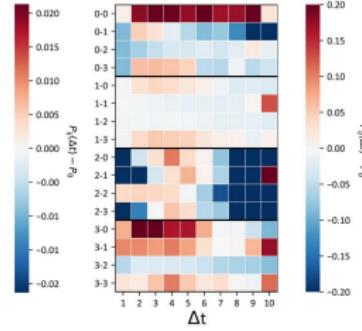
Twitter



Ads



PD



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# Conclusion

- Efficient convex model to investigate the way interactions happen within various datasets.
- Interactions modeling has been little explored in data science. Unlike previous models, our method accounts for both the interaction effects and their influence over time (the interaction profile).
- Better results on synthetic and various real-world datasets
- Possible applications in recommender systems, spreading processes, human choice behavior, etc.,

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# Thanks for your attention !